

Problem 1

Given $M_* = 3M_\odot$

By mass-luminosity relation, ~~$L \propto M^4$~~ $L = kM^4$ (k is a const.)

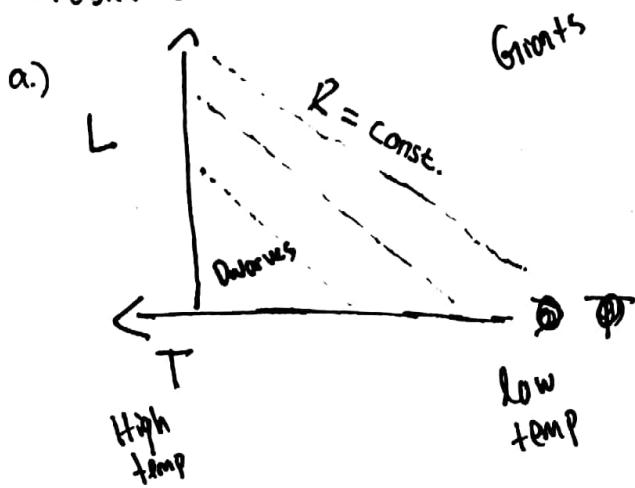
$$\frac{L_*}{L_\odot} = \frac{kM_*^4}{kM_\odot^4} = \frac{L_*}{L_\odot} = \left(\frac{M_*}{M_\odot}\right)^4$$

Plug in $M_* = 3M_\odot$

$$\frac{L_*}{L_\odot} = \left(\frac{3M_\odot}{M_\odot}\right)^4$$

$= 3^4$

Problem 2



Diagonal lines across HR diagram are lines of constant Radius.

X-axis traditionally reversed - sorry!

Consider a star in the top right corner. It has low T & high L .

By $L = 4\pi R^2 \sigma T^4$, if T is low, we must boost R to compensate, if we still want a large L .

b.) Plot color. What value can we use to represent color?

↓
Hot things are blue
Cold things are red

How about λ_{peak} ? $\lambda_{peak} = \frac{\text{const.}}{T}$
OR, Plot spectral type
OBAFGLM

So λ_{peak} & temp are basically interchangeable!

$$3. L = 4\pi R^2 \sigma T^4$$

if we double T , L increases by $2^4 \rightarrow L_A = 2^4 \cdot L_B$
 But L only represents intrinsic brightness — basically,
 what you would see if you were right next to the star.

As you move further away, apparent brightness decreases

$$\text{Apparent brightness} \propto \frac{1}{(\text{distance})^2}$$

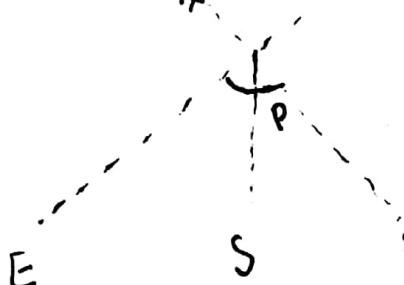
so, Star A is twice as far away, so it will appear $2^2 = 4$ times as dim. (or $\frac{1}{4}$ as bright)
 ↓ compared to Star B.

Therefore, its $\left(\frac{2^4}{4}\right)$ times as ~~brighter~~
brighter than that of Star B.
 ↓
 Apparent
 brightness
 is
 = 4
 = $\frac{16}{4}$

$$4. O B A F G K M$$

→ decreasing temp

F stars are hotter → shorter peak λ
 ★ ★



$$\Theta = 2\rho \quad [\text{by definition}] \quad (1)$$

$$\Theta = \frac{\lambda}{D} \quad [\text{resolution}] \quad (2)$$

$$\rho = \frac{1}{d} \quad (3)$$

When measuring parallax we are just measuring angular shift on sky → so, we are limited by angular resolution of our telescope.

• Plug (3) into (1)

$$\Theta = 2\left(\frac{1}{d}\right) = \frac{\lambda}{D}$$

$$\boxed{d = \frac{2D}{\lambda}}$$