

Type + Description

Visual / Astrometric

Resolve the 2 stars in binary & motion about each other

Observed Quantities

$$\alpha_1 = \frac{a_1 \cos i}{d}, \alpha_2 = \frac{a_2 \cos i}{d}$$

P (sit & watch)

Inferred Quantities

$$\frac{m_2}{m} = \frac{\alpha_1}{\alpha_2} = \frac{a_1}{a_2}$$

If d known, use Kepler III to get M_{total} & i → m_1, m_2 individually

Spectroscopic SINGLE lined

only 1 shift in spectrum due to motion of star around binary COM.

BUT one is much more luminous, so only see 1 line.

$$v_{1,r} = v_1 \sin i$$

P (from time to redshift → blueshift)

Mass function gives LOWER limit on companion mass m_2

$$m_2 \left(\frac{m_2}{m_1 + m_2} \right)^2 \sin^3 i = \frac{P}{2\pi G} v_{1,r}^3$$

MUST be ≤ 1
So set = 1 for lower limit on m_2

Spectroscopic DOUBLE lined

Two stars - equally luminous, so can detect 2 lines

$$v_{1,r} \neq v_{2,r}$$

P

$$\frac{m_1}{m_2} = \frac{v_{2,r}}{v_{1,r}} = \frac{a_2}{a_1}$$

(Kepler III) $M_{tot} = \frac{4\pi^2}{G P^3} (a_1 + a_2)^3$

Do we have a_1, a_2 ? Not quite, but we do measure them up to an inclination factor:

$$a_1 \sin i = \frac{P v_{1,r}}{2\pi} \quad \& \quad a_2 \sin i = \frac{P v_{2,r}}{2\pi}$$

all observables all observables

Spectroscopic ~~DOUBLE lined~~
Eclipsing

(one star passes in front of another)

Depth of light curve $F_0 - F_1$ & $F_0 - F_2$

Orbital period P
time btw eclipses

$$\text{Temp ratio: } \left(\frac{F_0 - F_2}{F_0 - F_1} \right) = \left(\frac{T_h}{T_c} \right)^4$$

BIC eclipsing, know immediately that $i = 90^\circ$
If v known (e.g., from spectra), then measure R_1